

High-quality factor Ta₂O₅-on-insulator resonators with ultimate thermal stability

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Experiments in photonics, laser optics and quantum technology require low loss, thermal and mechanical stability. While photonic integrated circuits on monolithic chips achieve interferometric stability, important nanophotonic material systems suffer from propagation loss, thermal drift and noise that prevent, for example, precise frequency stabilization of resonators. Here we show that tantalum pentoxide (Ta₂O₅) on insulator micro-ring resonators combine quality factors beyond 1.8 Mio. with vanishing temperature-dependent wavelength shift in the relevant 70 K to 90 K temperature range. Our Ta₂O₅-on-SiO₂ devices will thus enable athermal operation at liquid nitrogen temperatures, paving the way for ultra-stable low-cost resonators, as desired for wavelength division multiplexing, on chip frequency stabilization and low noise optical frequency comb generation.

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Performing experiments in ultra-low noise environments has become a crucial requirement in many branches of optics. State-of-the-art optical clocks, precision spectroscopy, nonlinear optics, and quantum technology implementations are extremely sensitive to both mechanical noise as well as thermal noise processes. This is exemplified by the enormous challenges involved in laser frequency stabilization with ultra-high quality factor (Q) Fabry-Perot cavities fabricated from ultra-low expansion glasses or even single crystal materials [1–3]. Photonic integrated circuits (PICs) allow for overcoming mechanical stability issues by fabricating resonators out of dielectric thin film systems on monolithic chips. While low cost and small device footprints due to strong mode confinement in high refractive index dielectrics constitute some advantages over bulk optic implementations, most PIC resonators suffer from noise introduced by variations in humidity, pressure, and, most importantly, temperature [4, 5]. The corresponding thermo-refractive noise of a PIC resonator is directly dependent on the thermo-optic and thermal expansion coefficients of the respective nanophotonic material system [6].

To realize stable micro-resonators with high quality factors a PIC platform further needs to achieve ultra-low optical loss.

Here we show that Tantalum Pentoxide-on-insulator (Ta₂O₅) PICs can satisfy these challenging demands when cooled to liquid nitrogen temperatures. Ta₂O₅ is emerging as a CMOS compatible nanophotonic material platform with optical properties that uniquely benefit a broad range of applications in metrology, nonlinear optics and quantum technologies [7–11]. Importantly, Ta₂O₅ offers high refractive index contrast to SiO₂, resulting in stable nanophotonic devices with compact footprints due to strong mode confinement [12–14]. Ta₂O₅ further features a wide transparency window from the ultraviolet to the infrared (0.28 μm–8 μm) [15], extremely low levels of intrinsic material fluorescence under optical excitation [16], negligible two photon absorption [17], and a relatively large third order optical nonlinearity. These features have allowed quantum emitter integration into Ta₂O₅ waveguides and the demonstration of nonlinear optical effects such as super continuum generation and spontaneous four wave mixing [18–21]. However, all applications to date have focused on room temperature operation, where thermo-refractive noise in Ta₂O₅-on-SiO₂ is comparable to other established nanophotonic platforms. Here, we investigate Ta₂O₅ on insulator micro-ring resonators over a large temperature range, extending the device operation down to 3 K. At liquid nitrogen temperatures we find minimal Temperature Dependent Wavelength Shift (TDWS) for wavelengths in the telecommunication C-band, thus giving rise to a new class of temperature stable high quality-factor devices with relaxed cooling requirements.

We assess the thermal stability of Ta₂O₅ PICs by extracting the TDWS of high-quality factor micro-ring resonances, which are cooled from room temperature to 3 K in a closed cycle cryostat. We employ spectroscopic ellipsometry (SE) of the Ta₂O₅-on-SiO₂ sample over a similar temperature range to determine the thermal expansion coefficient and then extract the thermo-optic coefficient from the TDWS measurements. This technique allows for separating the contributions of (Ta₂O₅) waveguide and (SiO₂) substrate on the thermal behavior of the device.

To best assess the intrinsic properties of Ta₂O₅ devices, we design micro-ring resonators for multi-mode operation, featuring wider waveguides in which fundamental propagation modes

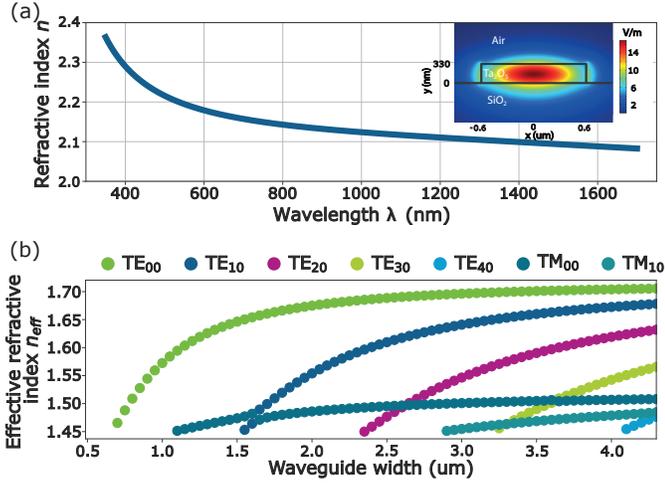


Fig. 1. (a) Refractive index of a Ta_2O_5 thin film, determined via multilayer modeling of spectroscopic ellipsometry. (inset) Simulated optical mode profile in a Ta_2O_5 ridge waveguide (b) FEM simulations of effective refractive indices for propagating modes in Ta_2O_5 waveguides of different width.

are less affected by scattering at waveguide sidewalls, leading to higher quality factors. We first record variable angle spectroscopic ellipsometer (VASE) data over a large wavelength range from 350 nm – 1800 nm at room temperature (Woolam M-2000) and fit a multilayer model to the ellipsometric spectra via regression analysis [22]. This procedure allows for extracting optical parameters such as refractive index $n(\lambda)$, extinction coefficient $\kappa(\lambda)$ and film thickness for each layer, which constitute essential input for nanophotonic device design. The resulting $n(\lambda)$ of the Ta_2O_5 film with a nominal thickness of 330 nm is shown in Figure 1 a. From electromagnetic field simulations using the finite element method (FEM, Comsol Multiphysics), we find that Ta_2O_5 waveguides of 330 nm \times 1.2 μm cross section on SiO_2 substrates predominantly support the fundamental transverse electric (TE₀₀) mode at 1550 nm wavelength, as shown in the inset of Figure 1 a, which we use as single-mode feed waveguides. Multimode operation up to TE₄₀, on the other hand, is possible in waveguides of 4 μm width, as shown in Figure 1 b, which we chose for the micro-ring resonators. To minimize bending loss, we chose to work with a micro-ring diameter of 150 μm .

We fabricate the micro-ring resonator devices, as shown in Figure 2 a, from 330 nm ion beam sputter deposited Ta_2O_5 thin films on a 3.3 μm buried oxide layer on a silicon handle wafer (thicknesses are nominal values). Grating couplers, waveguides and micro-ring resonators are patterned via electron beam lithography using a negative tone photoresist (ma-N 2403, micro resist technology) and reactive ion etching in CF_4 - CHF_3 -Ar chemistry. Each sample is annealed in oxygen enriched N_2 atmosphere at 600 $^\circ\text{C}$ for 6 h, which was found to notably reduce propagation loss of ion-beam sputtered Ta_2O_5 thin films [23–25], as can be inferred from determining the Q-factors of micro-ring resonators as a function of annealing temperature .

We characterize the resonator devices in transmission measurements with a sweep-laser in the telecom C-band (Toptica CTL-1500), as shown in Figure 2 b. For measurements in the 300 K to 3 K temperature range the chip is mounted inside a closed cycle cryostat (ICEOxford Dry ICE 1K) on a cryogenic 3-axes translation stage (Attocube ANPxyz101). The setup allows for

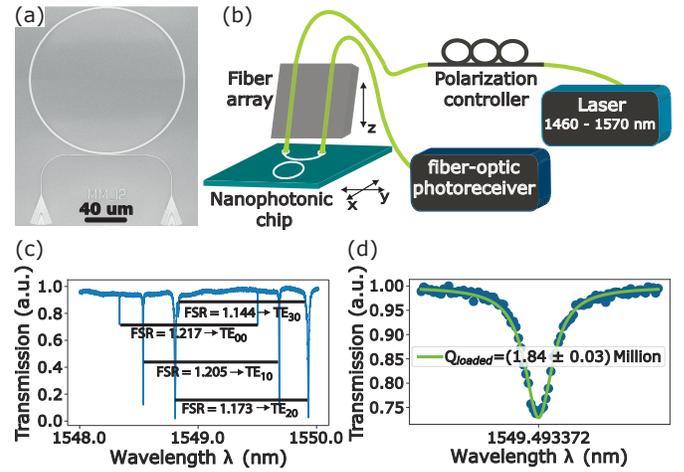


Fig. 2. (a) Scanning electron micrograph of a Ta_2O_5 -on-insulator ring resonator. (b) Setup for quality factor measurements and detection of the TDWS (c) Resonance spectrum of a ring resonator and corresponding resonator modes as extracted from the FSR. (d) Single resonance of a multimode waveguide with a loaded quality factor of approx. 1.8 Mio. The quality factor is obtained from fitting a Lorentzian line shape to the data.

positioning the grating couplers of a device under test under an optical fiber array, which also collects transmitted light for intensity measurements with a photodiode (NewFocus 2053-FC-M). The recorded spectra (see Figure 2 c) allow for identifying the modes guided inside the resonator by comparing experimentally observed free spectral ranges (FSR) with simulation results. For the TE₀₀ mode we find loaded quality factors up to $Q = 1.84$ Mio. from fitting a Lorentzian function to the data acquired with slightly over-coupled devices at room temperature, as shown in Figure 2 d.

The TDWS, given as [26]

$$\Delta\lambda \sim \frac{n_{\text{eff}}^{\alpha}}{n_{\text{eff},g}} \lambda \Delta T \quad (1)$$

describes fluctuation of the resonance wavelength λ of the micro-ring in terms of device temperature and the coefficient of thermal expansion (CTE) α that follows a $\frac{1}{L} \times \left(\frac{\delta L}{\delta T}\right)$ dependence on optical path length L inside the resonator. Here it is noteworthy that the optical mode extends from the Ta_2O_5 waveguide into the SiO_2 substrate (see Figure 1 a inset) and both material components contribute to the TDWS. We experimentally determine the TDWS $\Delta\lambda$ by following the center wavelength of a single high-Q-factor resonance when cooling the chip from room temperature to 3 K.

The data in Figure 3 a shows the resonance wavelength as determined from a Lorentzian fit to the transmitted power data for a large number of temperature values, measured at the backside of the sample. The TDWS is here expressed relative to the resonance wavelength at 3 K. Notably the gradient of the TDWS vanishes not only for temperatures < 15 K, where several quantum technology devices are being operated, but also in the 70 K – 90 K temperature range, which can conveniently be reached with economic liquid nitrogen (LN) cooling. In these temperature regions Ta_2O_5 -on- SiO_2 devices achieve ultimate thermal stability.

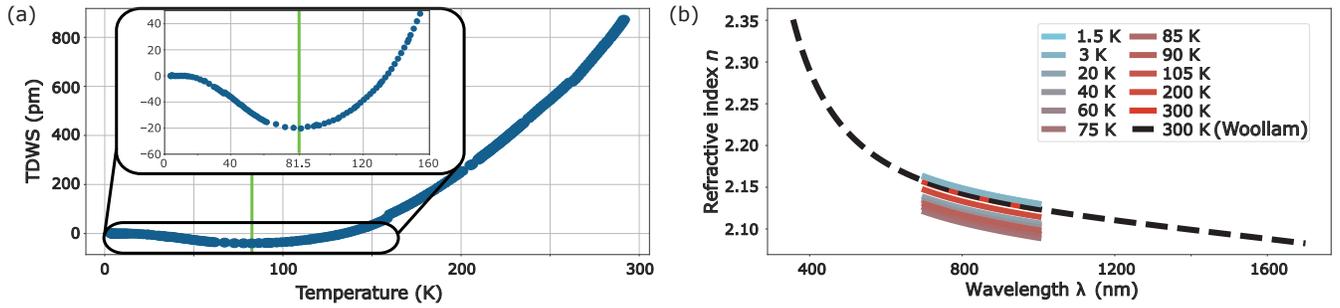


Fig. 3. (a) TDWS vs temperature. The measured resonance wavelength at 3 K serves as a reference for the TDWS at other temperatures. The inset shows a zoom in to temperature range around 80 K where the TDWS-gradient changes sign. (b) Refractive index of a Ta_2O_5 thin film for different temperatures determined from SE measurements (Accurion ellipsometer) from 1.5 K to room temperature. The data measured with the Woollam ellipsometer (same as Figure 1 a) is plotted to show the close agreement of the results from two different Ellipsometers accessing different wavelength ranges.

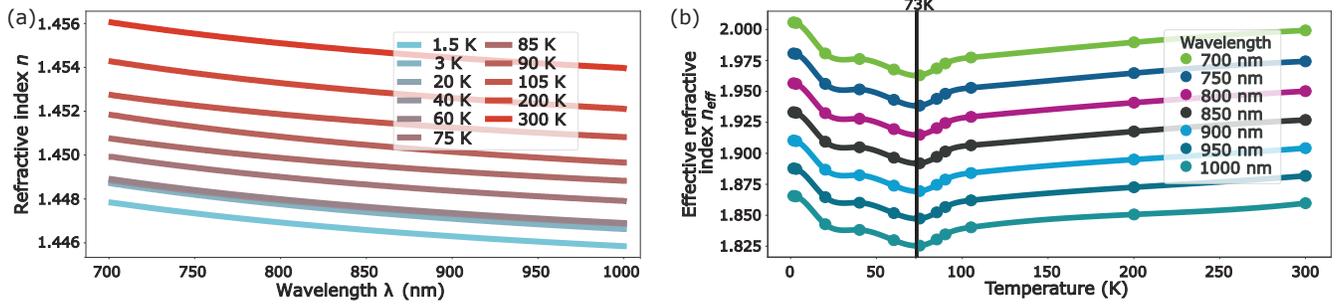


Fig. 4. (a) Refractive index of the SiO_2 substrate for different temperatures, measured from 1.5 K to room temperature with the Accurion SE. The data for SiO_2 and Ta_2O_5 are determined from the same ellipsometer measurement, thus enabling effective refractive index simulations. (b) Effective refractive index simulated via FEM for 1.2 μm wide, 330 nm thick Ta_2O_5 -on- SiO_2 waveguides.

To investigate the origin of this behavior, we combine the
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The refractive indices $n(\lambda)$ for the thin films are again deter-
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interaction in the measured wavelength range. The Eps-fix term
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Establishes the light dispersion in the high-energy limit with ϵ_∞ .
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largest material portion as compared to the 3.3 μm SiO_2 and 330 nm Ta_2O_5 thin films [28]. We note that the CTE of the silicon substrate is on the order of $1 \times 10^{-6} \text{K}^{-1}$ [29, 30], leading to a variation of a few nanometers over the 300 K temperature range, which has negligible influence on the effective refractive index of a nanophotonic device. In addition, SiO_2 and Ta_2O_5 are rather soft amorphous films and hence much less prone to strain caused by lattice mismatch.

On the other hand, the CTE has a noticeable effect on the coupling conditions and the free spectral range of the resonator even for small changes of the microring radius. Consequently, the thermal expansion coefficient α contributes considerably to the TDWS depicted in Figure 3 a. The corresponding functional behavior of the TDWS (see also Figure 4 b) resembles that of the slope of the expansion of silicon with a minimum at 85 K [29, 30]. From Equation 1 we conclude that the product of the CTE and the effective refractive index results in a shift of the global minimum in agreement with our measured TDWS. With effective refractive index and CTE reaching minimal values at 73 K and 85 K, respectively, we find optimal thermal device stability at 81.5 K. Realizations of thermally stable devices, such as the resonators considered here, will further benefit from slow variations of CTE, effective refractive index and TDWS around their respective minimal values, thus providing stable operation over an extended temperature range.

In summary, we show that Ta_2O_5 -on-insulator photonic integrated circuits allow for combining low-loss waveguiding with ultimate thermal stability. Optimal thermal conditions are found at 81.5 K by investigating the TDWS of a cryogenically cooled micro-ring resonator with loaded quality factors in excess of 1.8 Mio. Spectroscopic ellipsometry under cryogenic conditions provides evidence for the contributions of the temperature-dependent effective refractive index and CTE to the TDWS. Our results establish the Ta_2O_5 -on-insulator nanophotonic platform as an ideal choice for a wide range of applications requiring ultimate thermal stability, which is straightforwardly achievable at cost-efficient liquid nitrogen temperatures.

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Disclosures. The authors declare no conflicts of interest.

Data Availability Statement. Data underlying the results presented in this paper are not publicly available at this time but may be obtained from the authors upon reasonable request.

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